Tests Can't Be Handed Back Until Next Week



Almost looks like center of gravity!

How to determine your exact grade

.25*Final+.5*MidtermAvg+.1*HW+.05*Clickers+.1*Lab

If your goal is to get an A (90), solve for the variable "final" to see what you'd have to get on the final to make that happen.

Final test grade = [90-(.5*TestAvg +.1*HW+.05*Clickers+.1*Lab)]/0.25 And a lot of things can be approximated as springs!

Main Idea Today:

Springs



Summary of Today's Class

http://www.youtube.com/watch?v=-KqJXLJBb6s

Shocks

Pens

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Predict

A weight is suspended by a spring. The spring is then stretched until the weight is just above the eggs. When the spring is released, the weight is pulled up by the contracting spring and then falls back down under the influence of gravity. Ignoring air resistance, on the way down, it

- A. reverses its direction of travel well above the eggs
- B. reverses its direction of travel precisely as it reaches the eggs
- C. makes a mess as it crashes into the eggs (yuck)









The time to complete one cycle is called the period T.

Vertical Springs



When an 2.5 kg object is hung vertically on a certain light spring, the spring stretches to a distance y_o . What **force** does the spring apply to the object?

b) If the string stretches 2.76 cm from this mass, what is the force constant of the spring?c) What is the force if you stretch it 8 cm?

mg

F_s=ky_o

Free Body Diagram

> I might ask any of these on the test.

Spring (Elastic) Potential Energy

Elastic Potential Energy

When compressed or stretched, a spring gains elastic potential energy.





stratched

How Do We Find Spring Potential Energy?

$$F_S = -kx$$
 (Hooke's Law)
 $x = 0$ is equilibrium

$$W_C = -\Delta P E$$
$$W = F_{avg} \Delta x$$



If spring is compressed a distance x, average spring force is: $F_{S,average} = \frac{1}{2}(0-kx) = -\frac{1}{2}kx$ $\Rightarrow W_S = \overline{F}_{avg} x = (-\frac{1}{2}kx)x = -\frac{1}{2}kx^2$ $\Delta PE_{S} = PE_{2} - PE_{1} = -W_{S} = \frac{1}{2}kx^{2}$ $PE_1 = 0$, so $PE_S = \frac{1}{2}kx^2$

http://phet.colorado.edu/sims/mass-spring-lab/mass-spring-lab_en.html

A block is released from rest on a frictionless incline as shown. When the moving block is in contact with the spring and compressing it, what is happening to the gravitational potential energy PE_{grav} and the elastic potential energy PE_{el} ?



A. PE_{grav} and PE_{el} are both increasing.

- B. PE_{grav} and PE_{el} are both decreasing.
- C. PE_{grav} is increasing; PE_{el} is decreasing.
- D. PE_{grav} is decreasing; PE_{el} is increasing.
- E. The answer depends on how the block's speed is changing.



Amplitude of Oscillation

Amplitude (A) is maximum distance from equilibrium point

What is the velocity at this point? Only have potential energy





Energy in an oscillator

• Total energy of system (no frictional forces doing work):

$$E = KE + PE = \frac{1}{2}mv^{2} + \frac{1}{2}kx^{2}$$

- *E* is the same everywhere as KE increases PE decreases and vice-versa
- *E* in terms of amplitude: when x = A, v = 0

Velocity as a Function of Position (instead of time)

$$\frac{1}{2}mv^2 + \frac{1}{2}kx^2 = \frac{1}{2}kA^2$$

• Conservation of Energy allows a calculation of the velocity of the object at any position

$$v = \pm \sqrt{\frac{k}{m} \left(A^2 - x^2 \right)}$$

- Speed is a maximum at x = 0
- Speed is zero at $x = \pm A$
- The \pm indicates the object can be traveling in either direction







A spring with spring constant 300 N/m is attached to an object whose mass is 2.0 kg. If the spring is initially stretched A=0.25 m, what is the velocity of the object at x = 0, -*A* and *A*/2?



Previous Hard Test Question

A person who is still oscillating up and down **after** completing a bungee jump can be treated as a mass on a **vertical spring**, where gravity might also play a role. In this approximation, where is the magnitude of the **net acceleration** of the person in oscillation maximized? [Hint: Draw FBDs.]

A. The acceleration is always g=9.8 m/s².
B. At the equilibrium length of the bungee cord.
C. When the person is closest to the ground.
D. When the person is farthest from the ground.
E. Both when the person is closest and farthest from the ground.

Graphing the Motion of Springs

The paper moves at a constant speed underneath the pencil. If we were to graph what we observe, what would the position versus time graph look like?





D.



Graphing the Motion of Springs

The periodic motion of a spring is called sinusoidal motion, since it follows a sine or cosine relation.

This periodic motion is Simple Harmonic Motion.



Simple Harmonic Motion

- Any vibrating system with *F* proportional to *-x* like Hooke's law (F=-kx) undergoes SHM
- System is called a simple harmonic oscillator (SHO)
 - Ex: Spring; pendulum (for small amplitudes), a car stuck in a ditch being ``rocked out", a person on a swing, vibrating strings, even sound (Ch.14)!





Main Ideas in Class Today

After today's class, you should be able to:

- Use Hooke's Law to find the force on an object attached to a spring based on Δx (or vice versa)
- Determine the potential energy in a spring and the work done by a spring
- Apply conservation of energy principles to springs

Suggested Practice Problems: 5.34, 5.35, C13.1, C13.3, C13.11, 13.1, 13.3, 13.5, 13.9, 13.11, 13.17, 13.19, 13.21, 13.23, 13.25, 13.27, 13.31